

Statistics-Binomial Distribution

What is the Binomial Distribution?

The Binomial Distribution is a discrete probability distribution that models the number of successes in a fixed number of independent trials, where each trial has two possible outcomes (success or failure). It's a popular distribution used to analyze binary data.

Key Characteristics:

1. **Fixed Number of Trials:** The binomial distribution involves a fixed number of independent trials.
2. **Binary Outcomes:** Each trial has only two possible outcomes: success or failure.
3. **Constant Probability of Success:** The probability of success remains the same for each trial.
4. **Independent Trials:** The outcome of one trial does not affect the outcome of another.

Probability Mass Function (PMF)

The PMF for the Binomial Distribution is given by:

$$P(X = k) = \binom{n}{k} * (p^k) * ((1-p)^{(n-k)})$$

where:

- $P(X = k)$ is the probability of exactly k successes
- n is the fixed number of trials
- k is the number of successes ($0 \leq k \leq n$)
- p is the probability of success in each trial ($0 < p < 1$)
- $\binom{n}{k}$ is the binomial coefficient, which represents the number of ways to choose k items from a set of n distinct items.

Example:

Suppose we want to find the probability that a coin lands heads up exactly 3 times out of 5 tosses. We can use the Binomial Distribution with:

$n = 5$ (number of trials) $k = 3$ (number of successes, i.e., heads) $p = 0.5$ (probability of success in each trial, since the coin is fair)

Using the PMF formula, we get:

$$P(X = 3) = \binom{5}{3} * (0.5^3) * ((1-0.5)^2) = 10 * (0.125) * (0.25) = 0.3125$$

Therefore, the probability of getting exactly 3 heads out of 5 coin tosses is approximately 31.25%.

This example illustrates how the Binomial Distribution can be used to analyze binary data and calculate probabilities for a fixed number of independent trials with constant success probability.

Curated by Brajesh Kumar